

$$U_n := 230V \quad I_n := 26.0A \quad \omega_n := 150 \frac{\text{rad}}{\text{s}} \quad R_a := 1.1\Omega \quad L_a := 0.01H$$

$$\Sigma J := 0.32 \text{kg} \cdot \text{m}^2$$

$$U_b := U_n \quad I_b := I_n \quad \omega_b := \omega_n \quad 0.667 \cdot \omega_b = 100.05 \cdot \frac{\text{rad}}{\text{s}} \quad \Psi_{fn} := \frac{U_n - R_a \cdot I_n}{\omega_n}$$

$$\Psi_{fn} = 1.343 \text{ Wb}$$

$$M_{en} := \Psi_{fn} \cdot I_n = 34.909 \cdot \text{N} \cdot \text{m} \quad m_{mo} := 0.3 \cdot M_{en} = 10.473 \cdot \text{N} \cdot \text{m} \quad k := 0.0 \cdot \frac{M_{en}}{\omega_n} \quad k = 0$$

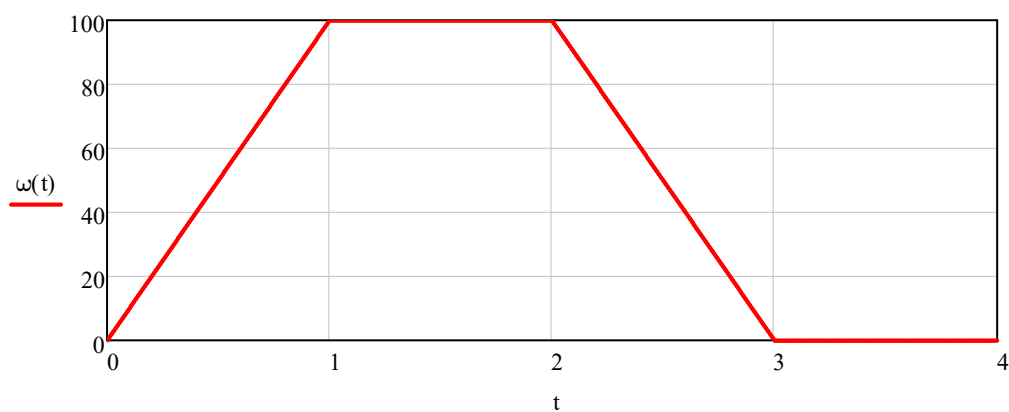
Željeni dijagram brzine:

Vreme nije normalizovano.

$$\omega(t) := \begin{cases} 0 & \text{if } t < 0s \\ \left(100 \cdot \frac{\text{rad}}{\text{s}^2} t \right) & \text{if } 0s \leq t < 1s \\ 100 \frac{\text{rad}}{\text{s}} & \text{if } 1s \leq t < 2s \\ \left[100 \frac{\text{rad}}{\text{s}} - 100 \cdot \frac{\text{rad}}{\text{s}^2} \cdot (t - 2s) \right] & \text{if } 2s \leq t < 3s \\ 0 & \text{if } t \geq 3s \end{cases}$$

$$m_m(t) := 0.3 \cdot M_{en} + k \cdot \omega(t)$$

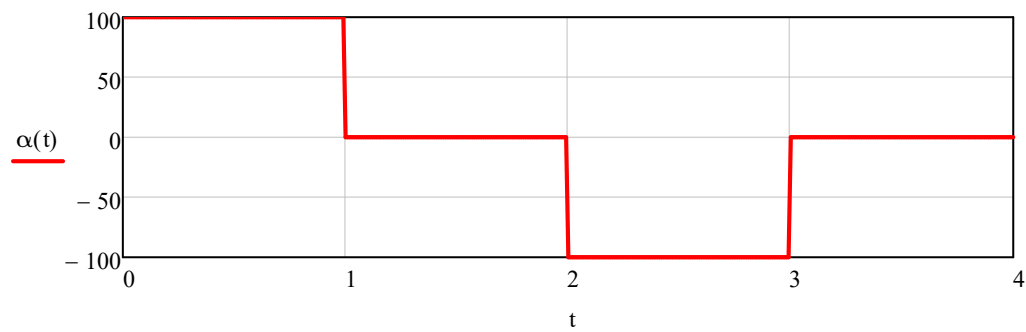
$$t := 0s, 0.01s.. 4s$$



Moment ima statički i dinamičku komponentu. Dinamička komponenta je proporcionalna ubrzanju.

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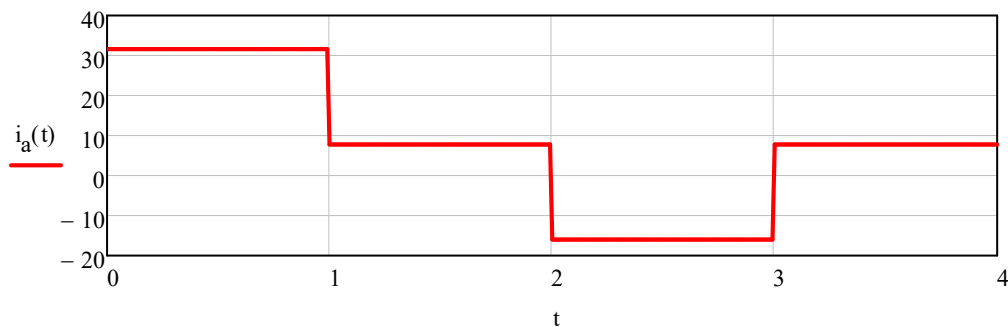
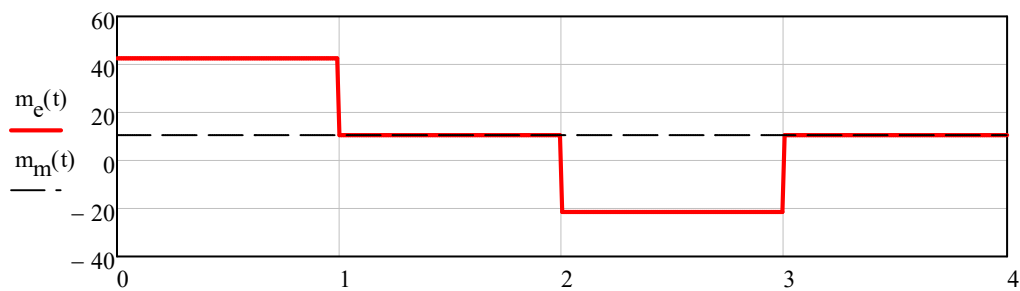
$$\alpha(t) := \begin{cases} 0 & \text{if } t < 0\text{s} \\ \left(100 \frac{\text{rad}}{\text{s}^2}\right) & \text{if } 0\text{s} \leq t < 1\text{s} \\ 0 & \text{if } 1\text{s} \leq t < 2\text{s} \\ \left(-100 \frac{\text{rad}}{\text{s}^2}\right) & \text{if } 2\text{s} \leq t < 3\text{s} \\ 0 & \text{if } t \geq 3\text{s} \end{cases} \quad \alpha(t) := \frac{d}{dt} \omega(t)$$



$$m_e(t) := m_m(t) + \sum J \cdot \alpha(t) \quad i_a(t) := \frac{m_e(t)}{\Psi_{fn}}$$

$m_e(0\cdot\text{s}) = 42.473 \cdot \text{N}\cdot\text{m}$ $m_e(0.99\cdot\text{s}) = 42.473 \cdot \text{N}\cdot\text{m}$ $m_e(1\cdot\text{s}) = 10.473 \cdot \text{N}\cdot\text{m}$ $m_e(1.99\cdot\text{s}) = 10.473 \cdot \text{N}\cdot\text{m}$
 $m_e(2\cdot\text{s}) = -21.527 \cdot \text{N}\cdot\text{m}$ $m_e(2.99\cdot\text{s}) = -21.527 \cdot \text{N}\cdot\text{m}$ $m_e(3\cdot\text{s}) = 10.473 \cdot \text{N}\cdot\text{m}$ $m_e(3.99\cdot\text{s}) = 10.473 \cdot \text{N}\cdot\text{m}$

$i_a(0\cdot\text{s}) = 31.633 \cdot \text{A}$ $i_a(0.99\cdot\text{s}) = 31.633 \cdot \text{A}$ $i_a(1.0\cdot\text{s}) = 7.8 \cdot \text{A}$ $i_a(1.99\cdot\text{s}) = 7.8 \cdot \text{A}$
 $i_a(2.0\cdot\text{s}) = -16.033 \cdot \text{A}$ $i_a(2.99\cdot\text{s}) = -16.033 \cdot \text{A}$ $i_a(3.0\cdot\text{s}) = 7.8 \cdot \text{A}$ $i_a(3.99\cdot\text{s}) = 7.8 \cdot \text{A}$

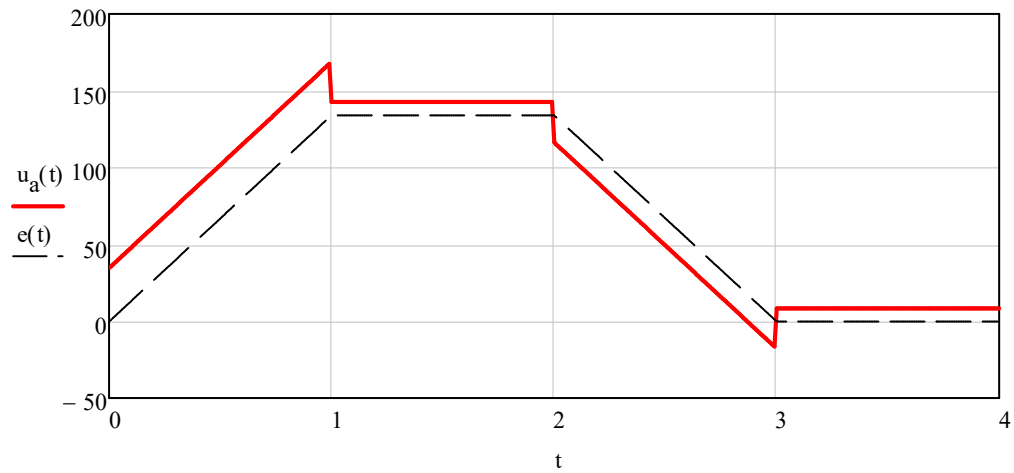


$$e(t) := \omega(t) \cdot \Psi_{fn}$$

$$u_a(t) := \omega(t) \cdot \Psi_{fn} + R_a \cdot i_a(t)$$

$$u_a(0) = 34.796 \text{ V} \quad u_a(0.999 \cdot s) = 168.929 \text{ V} \quad u_a(1 \cdot s) = 142.847 \text{ V} \quad u_a(1.99 \cdot s) = 142.847 \text{ V}$$

$$u_a(2.0 \cdot s) = 116.63 \text{ V} \quad u_a(2.99 \cdot s) = -16.294 \text{ V} \quad u_a(3.0s) = 8.58 \text{ V} \quad u_a(3.99s) = 8.58 \text{ V}$$



C)

$$i_{aC}(t) := \begin{cases} 7.8 \text{ A} & \text{if } t < 2 \text{ s} \\ 0 & \text{if } t \geq 2 \text{ s} \end{cases}$$

$$m_{eC}(t) := \begin{cases} \Psi_{fn} \cdot i_{aC}(t) & \text{if } t < 2 \text{ s} \\ 0 & \text{if } t \geq 2 \text{ s} \end{cases}$$

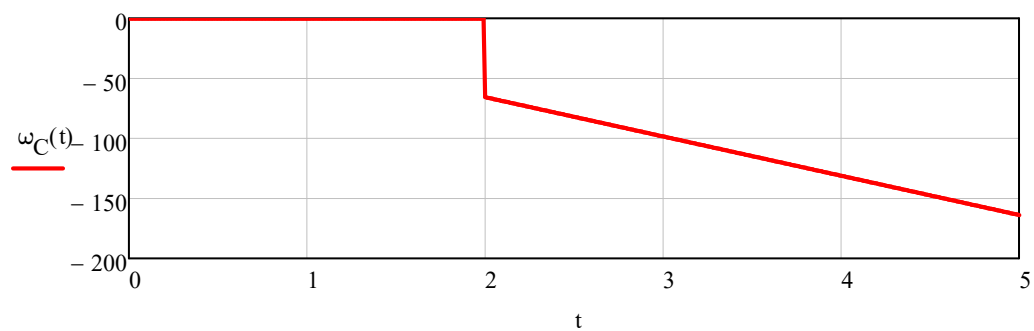
$$\alpha_C(t) := \begin{cases} 0 & \text{if } t < 2 \text{ s} \\ -\frac{m_m(t)}{\Sigma J} & \text{if } t \geq 2 \text{ s} \end{cases}$$

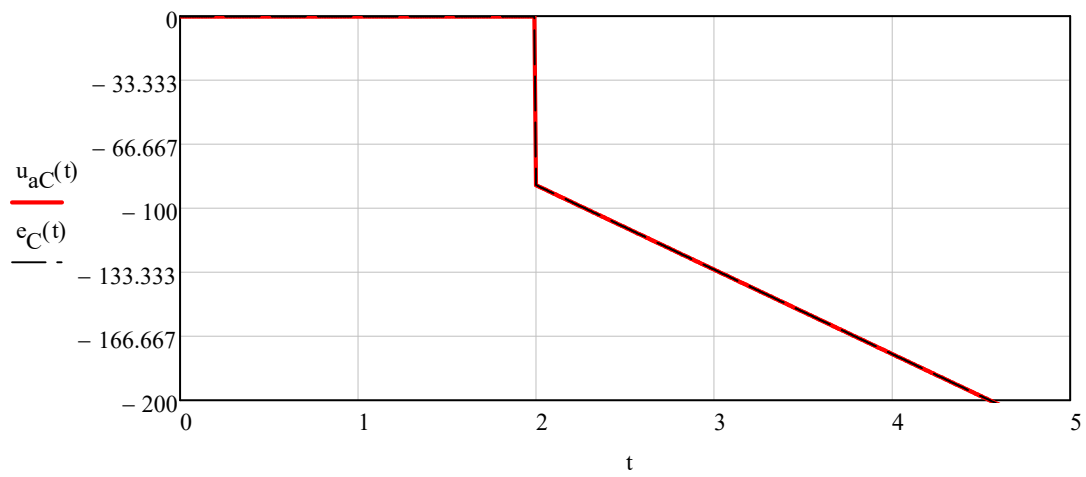
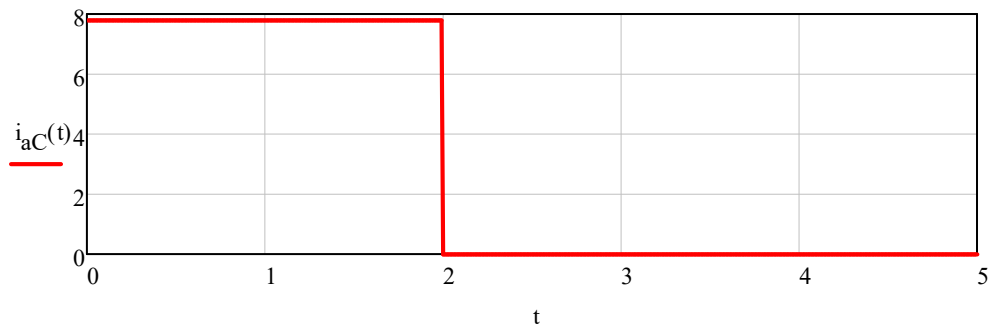
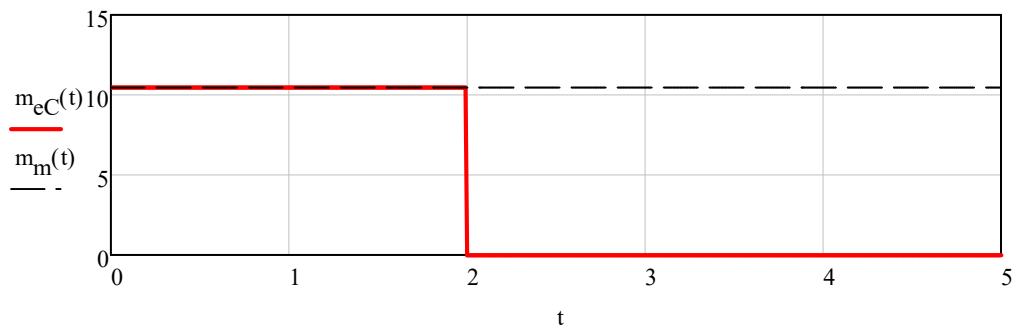
$$\omega_C(t) := \alpha_C(t) \cdot t$$

$$e_C(t) := \omega_C(t) \cdot \Psi_{fn}$$

$$u_{aC}(t) := e_C(t)$$

$$t := 0 \text{ s}, 0.01 \text{ s} \dots 5 \text{ s}$$





$$u_{aC}(4.5s) = -197.74 \text{ V}$$

$$U_{sn} := 220V \quad f_{sn} := 50Hz \quad \omega_{sn} := 2 \cdot \pi \cdot f_{sn} \quad o \equiv 2 \cdot \pi \text{ rad}$$

$$R_r := 2.5\Omega \quad \lambda_s := 8.8mH \quad \lambda_r := \lambda_s \quad s_n := \frac{1500 - 1400}{1500} = 0.0667 \quad P := 2$$

$$\omega_b := \omega_{sn} \quad U_b := U_{sn} \quad \underline{\underline{J}} := 1kg \cdot m^2$$

$$I_n := \frac{U_{sn}}{\sqrt{\left(\frac{R_r}{s_n}\right)^2 + \omega_{sn}^2 \cdot (\lambda_s + \lambda_r)^2}} = 5.8039 \text{ A} \quad M_b := \frac{3 \cdot U_b \cdot I_n}{\frac{\omega_b}{P}} = 24.3863 \cdot N \cdot m$$

$$T_m := J \cdot \frac{\omega_b}{M_b} = 12.8826 \text{ s} \quad Z_b := \frac{U_b}{I_n} = 37.9054 \Omega \quad L_b := \frac{Z_b}{\omega_b}$$

$$\lambda_e := \frac{\lambda_s + \lambda_r}{L_b} = 0.1459 \quad \underline{\underline{R_e}} := \frac{R_r}{Z_b} = 0.066 \quad \omega_n := \frac{1400}{1500} = 0.9333 \quad \omega_n \cdot \frac{\omega_b}{P} = 146.6077 \cdot \frac{\text{rad}}{\text{s}}$$

$$\omega_{rpr} := \frac{R_r}{\lambda_e} = 0.4521 \quad \omega_{rpr} \cdot \omega_b = 142.0455 \cdot \frac{\text{rad}}{\text{s}} \quad m_{pr} := \frac{1}{2 \cdot \lambda_e} = 3.4277 \quad m_{pr} \cdot M_b = 83.59 \cdot N \cdot m$$

$$U_s(\omega_s) := \begin{cases} \left(\frac{U_{sn}}{\omega_{sn}} \cdot \omega_s\right) & \text{if } 0 < \omega_s < \omega_{sn} \\ U_{sn} & \text{otherwise} \end{cases} \quad U_s(\omega_s) := \begin{cases} \omega_s & \text{if } 0 < \omega_s < 1 \\ 1 & \text{otherwise} \end{cases}$$

$$m_e(\omega_s, \omega_r) := \frac{R_r \cdot \omega_r}{R_r^2 + \omega_r^2 \cdot (\lambda_e)^2} \quad i_s(\omega_s, \omega_r) := \frac{U_s(\omega_s)}{\sqrt{\left(R_r \cdot \frac{\omega_s}{\omega_r}\right)^2 + \omega_s^2 \cdot \lambda_e^2}} \quad I_s(\omega_s, \omega_r) := \frac{U_s(\omega_s)}{R_r \cdot \frac{\omega_s}{\omega_r} + i \cdot \omega_s \cdot \lambda_e}$$

$$\omega_{sA} := \frac{30Hz}{50Hz} = 0.6 \quad \omega_r := -2, -1.99 \dots 1 \quad \omega_{rn} := 1 - \omega_n = 0.0667 \quad \omega_{rn} \cdot \omega_b = 20.944 \cdot \frac{\text{rad}}{\text{s}}$$

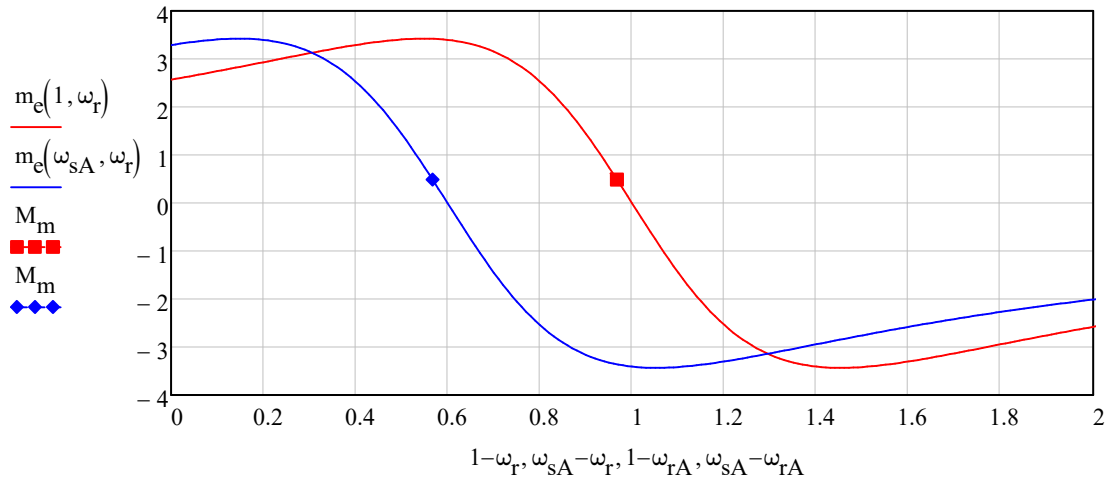
$$M_{en} := m_e(1, \omega_{rn}) = 0.9893 \quad M_{en} \cdot M_b = 24.1254 \cdot N \cdot m \quad \omega_{sA} \cdot \frac{\omega_b}{P} = 900 \cdot \frac{o}{\text{min}}$$

$$M_m := \frac{1}{2} \cdot M_{en} \quad M_m \cdot M_b = 12.0627 \cdot N \cdot m \quad M_m = 0.4947$$

$$\omega_{rx} := 0.001 \quad \text{Given} \quad m_e(\omega_{sn}, \omega_{rx}) = M_m \quad \omega_{rA} := \text{Find}(\omega_{rx}) = 0.0328 \quad \text{Rešava se kvadratna jednačina.}$$

$$\omega_A := \omega_{sA} - \omega_{rA} = 0.5672 \quad \omega_A \cdot \frac{\omega_b}{P} = 89.0962 \cdot \frac{\text{rad}}{\text{s}} \quad \omega_A \cdot \frac{\omega_b}{P} = 850.8064 \cdot \frac{o}{\text{min}}$$

$$i_{sA} := i_s(\omega_{sA}, \omega_{rA}) = 0.496 \quad i_{sA} \cdot I_n = 2.8785 \text{ A} \quad U_s(\omega_{sA}) = 0.6 \quad U_s(\omega_{sA}) \cdot U_{sn} = 132 \text{ V}$$



$$\Delta\omega_{s,\min} := \omega_{rA}$$

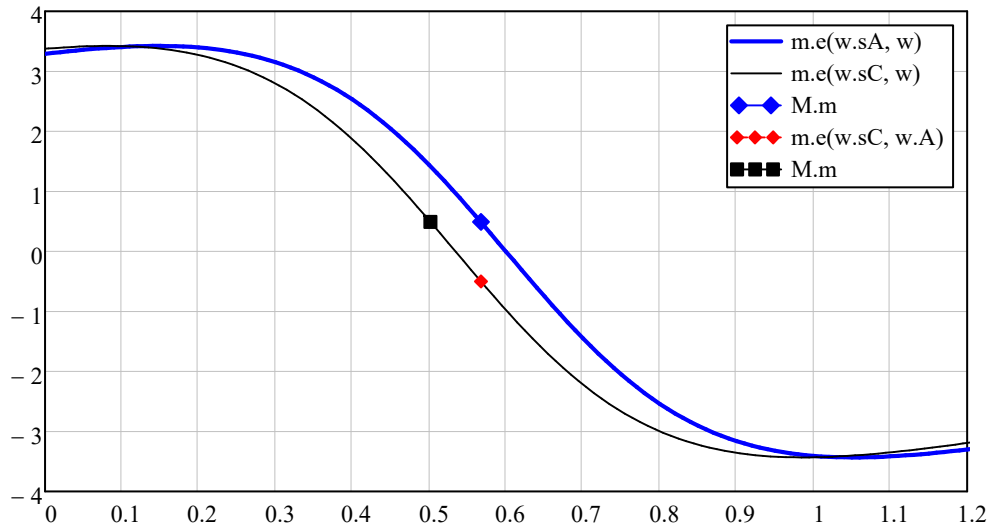
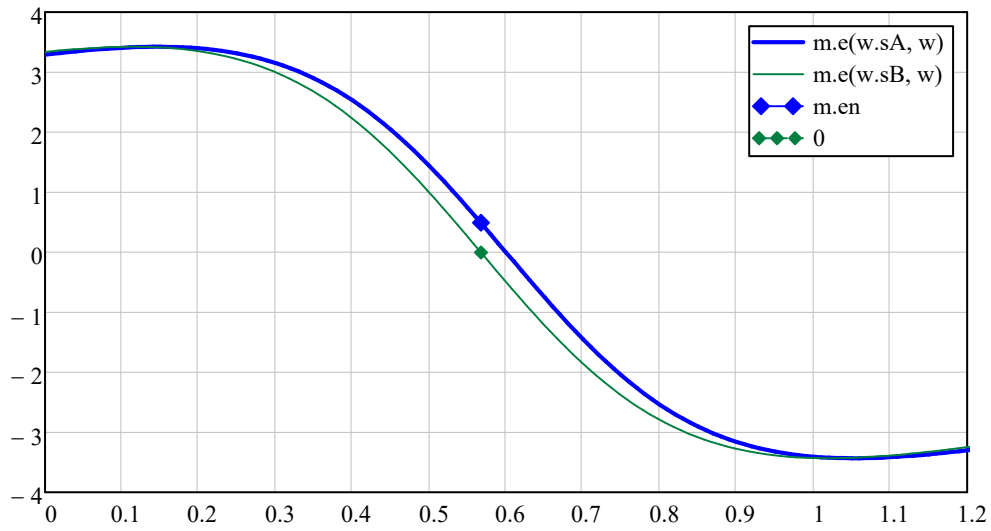
$$\Delta\omega_{s,\min} \cdot \omega_b = 10.3031 \cdot \frac{\text{rad}}{\text{s}}$$

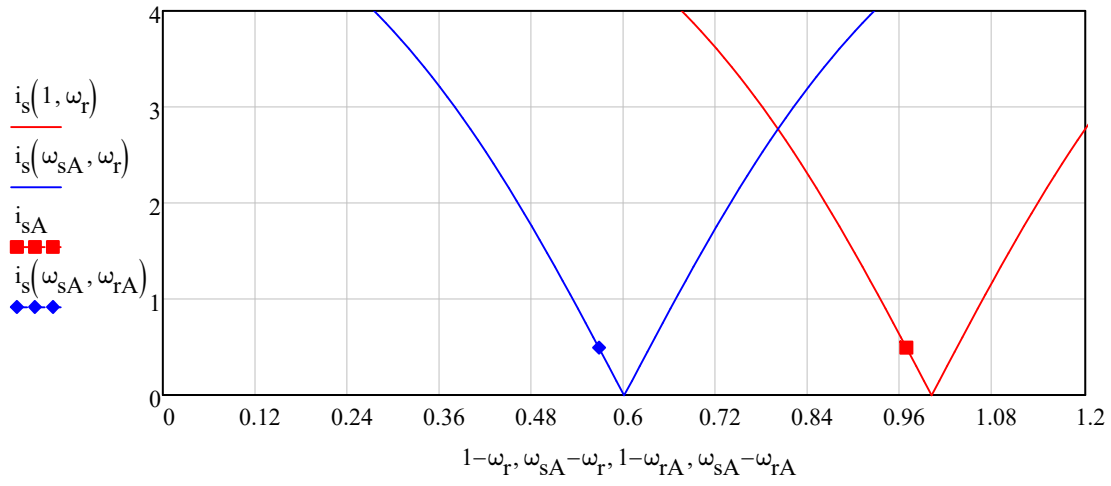
$$\Delta\omega_{s,\min} \cdot 50\text{Hz} = 1.6398 \cdot \text{Hz}$$

$$\omega_{sB} := \omega_{sA} - \Delta\omega_{s,\min} = 0.5672$$

$$\omega_{sC} := \omega_{sA} - 2\Delta\omega_{s,\min} = 0.5344$$

$$\omega_C := \omega_{sC} - \omega_{rA} = 0.5016$$





$$f_{sA} := 35\text{Hz}$$

$$f_{sB} := f_{sA} - \Delta\omega_{s,\min} \cdot f_{sn} = 33.3602 \cdot \text{Hz}$$

$$\omega_{sC} \cdot \omega_b = 167.8894 \cdot \frac{\text{rad}}{\text{s}}$$

$$m_e(\omega_{sC}, \omega_{sC} - \omega_A) \cdot M_b = -12.0627 \cdot \text{N} \cdot \text{m}$$

$$m_e(\omega_{sC}, \omega_{sC} - \omega_C) \cdot M_b = 12.0627$$

