

$$U_n := 220V \quad I_n := 55A \quad \omega_n := 150 \frac{\text{rad}}{\text{s}} \quad R_a := 0.091\Omega \quad L_a := 0.007H$$

$$\Sigma J := 1.067 \text{kg} \cdot \text{m}^2$$

$$U_b := U_n \quad I_b := I_n \quad \omega_b := \omega_n \quad \Psi_{fn} := \frac{U_n - R_a \cdot I_n}{\omega_n}$$

$$\Psi_{fn} = 1.433 \text{Wb} \quad R_{ab} := \frac{U_b}{I_b}$$

$$M_{en} := \Psi_{fn} \cdot I_n = 78.832 \text{N} \cdot \text{m} \quad m_{mp} := M_{en} \cdot 0.4 = 31.533 \text{N} \cdot \text{m} \quad m_{mr} := M_{en} \cdot 0.1 = 7.883 \text{N} \cdot \text{m}$$

Željeni dijagram brzine: Vreme nije normalizovano.

$$\omega(t) := \begin{cases} 0 & \text{if } t < 0s \\ \left( 50 \cdot \frac{\text{rad}}{\text{s}^2} t \right) & \text{if } 0s \leq t < 1s \\ 50 \frac{\text{rad}}{\text{s}} & \text{if } 1s \leq t < 2s \\ \left[ 50 \frac{\text{rad}}{\text{s}} - 50 \cdot \frac{\text{rad}}{\text{s}^2} \cdot (t - 2s) \right] & \text{if } 2s \leq t < 3s \\ 0 & \text{if } t \geq 3s \end{cases}$$

Momenat opterećenja sastoji se od dve komponente

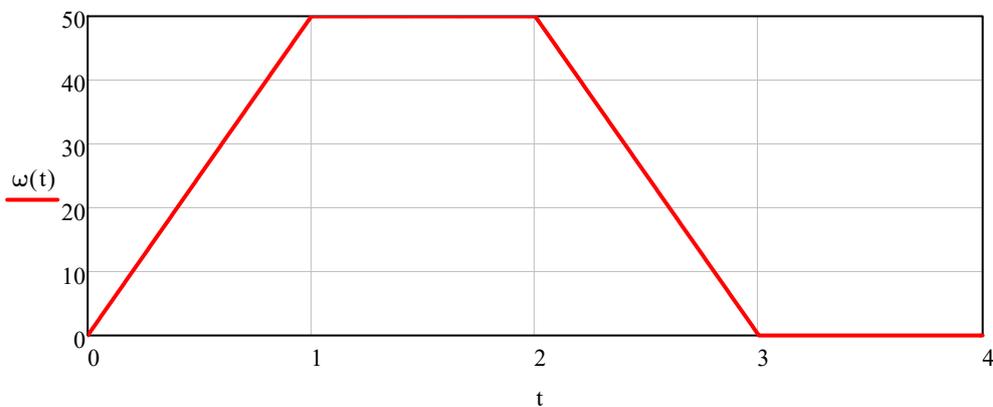
$$m_{m1} := m_{mp} \quad \text{Potencijalne prirode}$$

Na uzbrdici, m.m1 je pozitivno,  
na nizbrdici m.m1 je negativno

$$m_{m2}(t) := m_{mr} \cdot \text{sign}(\omega(t)) \quad \text{Reaktivne prirode}$$

$$m_m(t) := m_{m1} + m_{m2}(t)$$

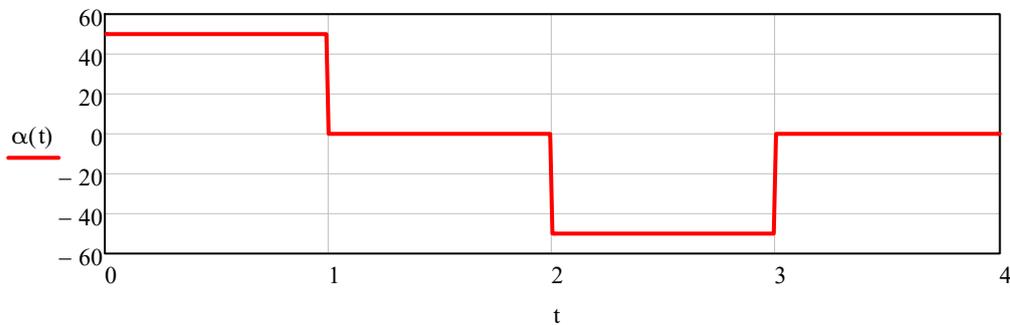
$$t := 0s, 0.01s .. 4s$$



Moment ima statički i dinamičku komponentu. Dinamička komponenta je proporcionalna ubrzanju.

$$\alpha(t) := \frac{d}{dt} \omega(t) \quad \blacksquare$$

$$\alpha(t) := \begin{cases} 0 & \text{if } t < 0 \text{ s} \\ \left( 50 \frac{\text{rad}}{\text{s}^2} \right) & \text{if } 0 \text{ s} \leq t < 1 \text{ s} \\ 0 & \text{if } 1 \text{ s} \leq t < 2 \text{ s} \\ \left( -50 \frac{\text{rad}}{\text{s}^2} \right) & \text{if } 2 \text{ s} \leq t < 3 \text{ s} \\ 0 & \text{if } t \geq 3 \text{ s} \end{cases}$$



$$m_e(t) := m_m(t) + \sum J \cdot \alpha(t) \quad i_a(t) := \frac{m_e(t)}{\Psi_{fn}}$$

$$m_e(0 \cdot \text{s}) = 84.883 \cdot \text{N} \cdot \text{m} \quad m_e(0.99 \cdot \text{s}) = 92.766 \cdot \text{N} \cdot \text{m} \quad m_e(1 \cdot \text{s}) = 39.416 \cdot \text{N} \cdot \text{m} \quad m_e(1.99 \cdot \text{s}) = 39.416 \cdot \text{N} \cdot \text{m}$$

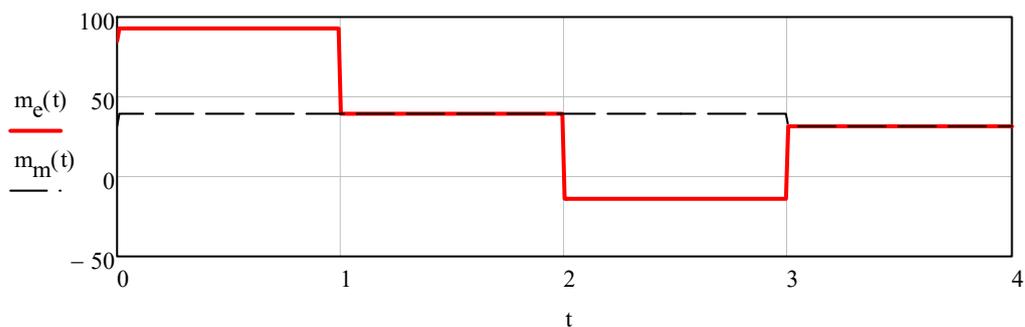
$$m_e(2 \cdot \text{s}) = -13.934 \cdot \text{N} \cdot \text{m} \quad m_e(2.99 \cdot \text{s}) = -13.934 \cdot \text{N} \cdot \text{m} \quad m_e(3 \cdot \text{s}) = 31.533 \cdot \text{N} \cdot \text{m} \quad m_e(3.99 \cdot \text{s}) = 31.533 \cdot \text{N} \cdot \text{m}$$

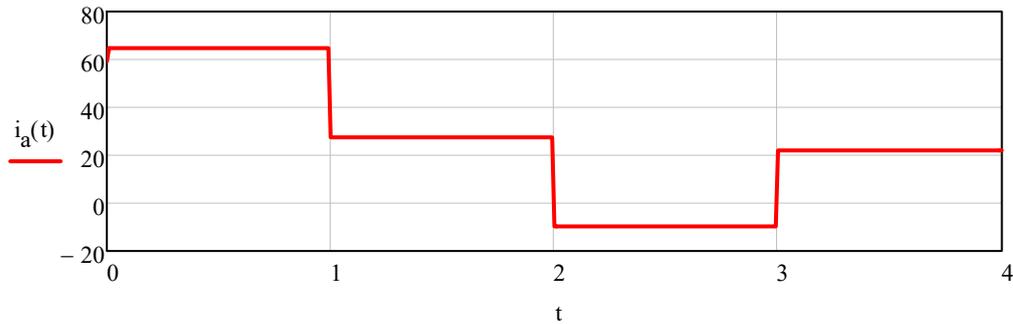
$$i_a(0 \cdot \text{s}) = 59.222 \cdot \text{A} \quad i_a(0.99 \cdot \text{s}) = 64.722 \cdot \text{A} \quad i_a(1.0 \cdot \text{s}) = 27.5 \cdot \text{A} \quad i_a(1.99 \cdot \text{s}) = 27.5 \cdot \text{A}$$

$$i_a(2.0 \cdot \text{s}) = -9.722 \cdot \text{A} \quad i_a(2.99 \cdot \text{s}) = -9.722 \cdot \text{A} \quad i_a(3.0 \cdot \text{s}) = 22 \cdot \text{A} \quad i_a(3.99 \cdot \text{s}) = 22 \cdot \text{A}$$

$$m_m(0 \cdot \text{s}) = 31.533 \cdot \text{N} \cdot \text{m} \quad m_m(0.99 \cdot \text{s}) = 39.416 \cdot \text{N} \cdot \text{m} \quad m_m(1 \cdot \text{s}) = 39.416 \cdot \text{N} \cdot \text{m} \quad m_m(1.99 \cdot \text{s}) = 39.416 \cdot \text{N} \cdot \text{m}$$

$$m_m(2 \cdot \text{s}) = 39.416 \cdot \text{N} \cdot \text{m} \quad m_m(2.99 \cdot \text{s}) = 39.416 \cdot \text{N} \cdot \text{m} \quad m_m(3 \cdot \text{s}) = 31.533 \cdot \text{N} \cdot \text{m} \quad m_m(3.99 \cdot \text{s}) = 31.533 \cdot \text{N} \cdot \text{m}$$



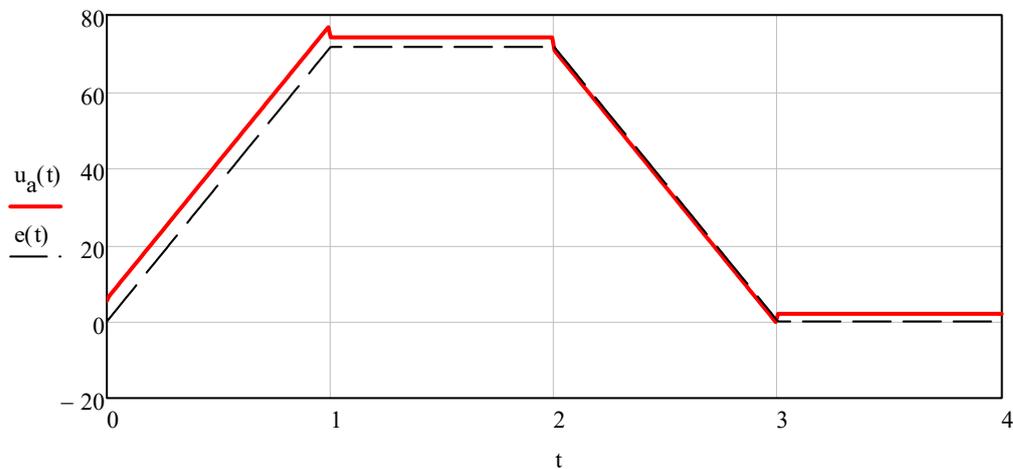


$$e(t) := \omega(t) \cdot \Psi_{fn}$$

$$u_a(t) := \omega(t) \cdot \Psi_{fn} + R_a \cdot i_a(t)$$

$$u_a(0) = 5.389 \text{ V} \quad u_a(0.999 \cdot s) = 77.483 \text{ V} \quad u_a(1 \cdot s) = 74.168 \text{ V} \quad u_a(1.99 \cdot s) = 74.168 \text{ V}$$

$$u_a(2.0 \cdot s) = 70.78 \text{ V} \quad u_a(2.99 \cdot s) = -0.168 \text{ V} \quad u_a(3.0 \cdot s) = 2.002 \text{ V} \quad u_a(3.99 \cdot s) = 2.002 \text{ V}$$



$$c) \quad i_{aC}(t) := \begin{cases} 27.5 \text{ A} & \text{if } t < 2 \text{ s} \\ 0 & \text{if } t \geq 2 \text{ s} \end{cases} \quad m_{eC}(t) := \begin{cases} \Psi_{fn} \cdot i_{aC}(t) & \text{if } t < 2 \text{ s} \\ 0 & \text{if } t \geq 2 \text{ s} \end{cases}$$

Od trenutka isključenja, do vremena  $t_x$  brzina je pozitivna ali opada zato što su obe komponente momenta opterećenja istog znaka. U trenutku  $t_x$  brzina je jednaka 0, a posle toga, potencijalna komponenta momenta pomaže kretanju, a reaktivna koči, tj.  $m_p$  je pozitivno, a  $m_r$  negativno i brzina motora postaje negativna, tj. transportni uređaj ubrzava na nizbrdici. Zato je potrebno aktivirati mehaničke kočnice u trenutku kada je brzina postala jednaka 0.

$$t_x := \frac{50 \cdot \frac{\text{rad}}{\text{s}} \cdot \Sigma J}{m_{mp} + m_{mr}}$$

$$t_x = 1.354 \text{ s}$$

Motor će se zaustaviti posle vremena  $t_1$ , a zatim će da nastavi da se ubrzava u suprotnom smeru, dok transportni uređaj ne dođe do podnožje uzbrdice kada će se potencijalna komponenta momenta opterećenja izjednačiti sa 0, a kretanje će da traje sve dok se sva kinetička energija uređaja ne potroši na savlađivanje reaktivne komponente opterećenja.

$$t_1 := 2 \cdot s + t_x$$

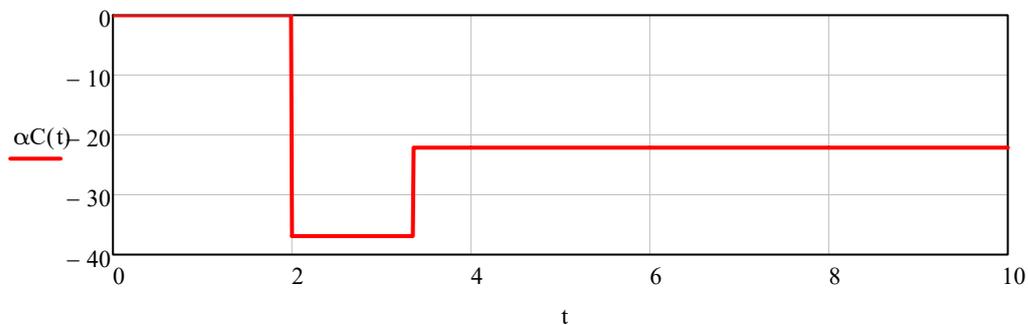
$$t_1 = 3.354 \text{ s}$$

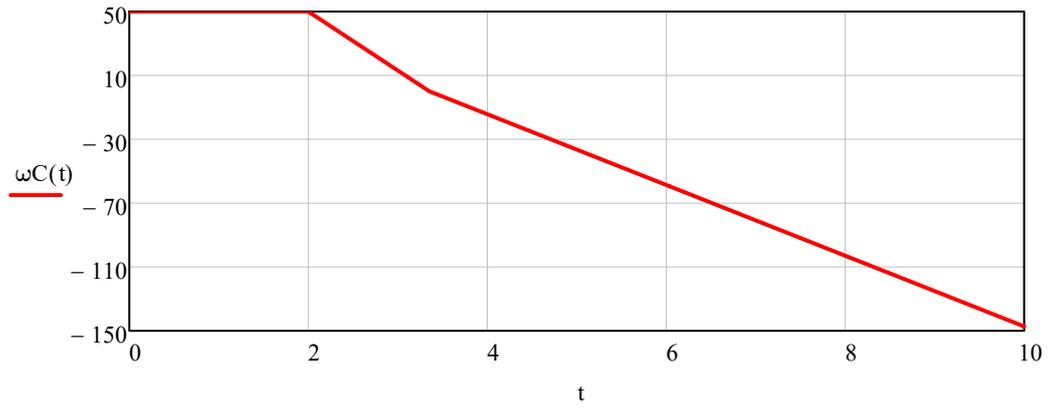
$$m_{mC}(t) := \begin{cases} m_{mp} + m_{mr} & \text{if } t < t_1 \\ m_{mp} - m_{mr} & \text{if } t \geq t_1 \end{cases}$$

$$\alpha_C(t) := \begin{cases} 0 & \text{if } t < 2s \\ -\frac{m_{mC}(t)}{\Sigma J} & \text{if } t \geq 2s \end{cases}$$

$$\omega_C(t) := \begin{cases} 50 \frac{\text{rad}}{\text{s}} & \text{if } t < 2s \\ 50 \frac{\text{rad}}{\text{s}} + \alpha_C(t) \cdot (t - 2 \cdot s) & \text{if } 2s \leq t < t_1 \\ 50 \frac{\text{rad}}{\text{s}} + \alpha_C \left( 2 \cdot s + \frac{t_x}{2} \right) \cdot t_x + \alpha_C(t) \cdot (t - t_1) & \text{if } t_1 \leq t \end{cases}$$

$$t := 0s, 0.01s.. 10s$$





$$e_C(t) := \omega_C(t) \cdot \Psi_{fn} \quad u_{aC}(t) := e_C(t)$$

$t := 0s, 0.01s .. 10s$

